# **Confinement effects on glass forming liquids probed by dynamic mechanical analysis**

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Many molecular glass forming liquids show a shift of the glass transition  $T<sub>g</sub>$  to lower temperatures when the liquid is confined into mesoporous host matrices. Two contrary explanations for this effect are given in literature: First, confinement induced acceleration of the dynamics of the molecules leads to an effective downshift of  $T<sub>g</sub>$  increasing with decreasing pore size. Second, due to thermal mismatch between the liquid and the surrounding host matrix, negative pressure develops inside the pores with decreasing temperature, which also shifts  $T_g$  to lower temperatures. Here we present dynamic mechanical analysis measurements of the glass forming liquid salol in Vycor and Gelsil with pore sizes of *d*=2.6, 5.0 and 7.5 nm. The dynamic complex elastic susceptibility data can be consistently described with the assumption of two relaxation processes inside the pores: A surface induced slowed down relaxation due to interaction with rough pore interfaces and a second relaxation within the core of the pores. This core relaxation time is reduced with decreasing pore size *d*, leading to a downshift of  $T_g \propto 1/d$  in perfect agreement with recent differential scanning calorimetry (DSC) measurements. Thermal expansion measurements of empty and salol filled mesoporous samples revealed that the contribution of negative pressure to the downshift of  $T_g$  is small (<30%) and the main effect is due to the suppression of dynamically correlated regions of size  $\xi$  when the pore size *d* approaches  $\xi$ .

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## **I. INTRODUCTION**

When approaching a glass transition some physical properties like viscosity or relaxation times change up to 14 or-ders of magnitude.<sup>1[,2](#page-7-4)</sup> An explanation for the observed slowing down of the dynamics is the formation of collectively dynamically rearranging clusters $3,4$  $3,4$  or regions, with growing size  $\xi$  and increasing relaxation times as  $T_g$  is approached.<sup>5</sup> The idea of an increasing dynamic correlation length  $\xi$  when approaching a glass transition is strongly supported by recent computer simulations, $6-8$  $6-8$  although not strictly proven, since computer simulations cannot treat the time range of the  $\alpha$ -process. Very recently a breakthrough was achieved in this field. Biroli *et al.*[9](#page-7-10) found first-time evidence that the mode coupling theory predicts a growing dynamic length scale approaching the glass transition of a supercooled liquid. The authors obtained a rather modest growth of the dynamical length scale  $\xi$  with decreasing temperature, which is in very good agreement with computer simulations $\delta$  and experimental results. Indeed many experimental setups like heat capac-ity spectroscopy,<sup>10,[11](#page-7-12)</sup> multidimensional NMR,<sup>12–[14](#page-8-0)</sup> multipoint dynamical susceptibilities, $15$  etc. have been used to monitor a possible growing length scale accompanying the glass transition. All these results agree in the fact that the obtained dynamically correlated regions—although material dependent—are on the order of 1–4 nm and display—if at all—a weak temperature dependence.

An alternative experimental approach to get a reference to a possibly existing cooperation length  $\xi$  which increases when  $T \rightarrow T_g$  is by spatial limitation of a glass forming liquid. Spatially confining geometries as ultrathin films, mesoporous silica or zeolithes have already been used to study phase transitions of water,<sup>16</sup> hydrocarbons,<sup>17</sup> noble gases,<sup>18[,19](#page-8-5)</sup> liquid crystals $20$  or alkenes.<sup>21</sup> But this concept also illuminated the old and still open question on the very nature of the glass transition and its dynamics: $^{22}$  In a pioneering work Jackson and McKenna<sup>23</sup> studied the glass transition of organic liquids in controlled pore glasses (CPG) for various pore sizes *d*. They found a reduction of the glass transition temperature  $T_g$  for liquids in confinement as compared to the bulk material. The downshift of  $T_g$  was larger for smaller pore sizes, i.e.,  $\Delta T_g \propto 1/d$ , an effect similar but not as strong as the suppression known for the melting temperature  $T_m$  in confinement. During the following two decades this effect was studied via calorimetry,  $24.25$  dielectric spectroscopy,  $26$ neutron scattering, $27$  light scattering, $28$  and molecular dynamics[.29](#page-8-15) It was shown that in many cases confinement below a characteristic length impedes<sup>24</sup> the transition, implying that molecules within a region of the size  $\xi$  (approaching  $T_g$  typically some  $nm^{30,31}$  $nm^{30,31}$  $nm^{30,31}$ ) have to cooperate and rearrange in order to create the glassy state. Hindering this cooperation first leads to a downshift of  $T_g$  if  $d \sim \xi_g$  and finally to a suppression of the transition if  $d < \xi_g$ .<sup>[24](#page-8-10)</sup>

However, although this shift of  $\tilde{T}_g$  with decreasing confinement size was found in numerous studies, there are complications which blur this simple picture: e.g., in many molecular dynamics simulations of glass forming liquids at high temperatures above the empirical mode-coupling temperature  $T_c$  confinement is found to slow down the dynamics.<sup>32[,33](#page-8-19)</sup> Furthermore, in some systems a competition appears between slowing down of molecular motions due to pinning of the molecules at the pore surface and acceleration of the dynamics due to decreasing size of the confinement. Another effect occurs due to the difference in thermal expansion coefficients of the porous host matrix and the glass forming liquid. This may create negative pressure upon the confined liquid when the glass transition is approached. Some authors attribute the whole observed downshift of  $T<sub>g</sub>$  to this negative pressure effect.<sup>28</sup> We will address these points in more detail below. For excellent reviews about these topics the reader is referred to Refs. [34](#page-8-20) and [35.](#page-8-21)

Very recently the confinement effect on the glass forming liquid salol was studied via dynamic mechanic analysis

TABLE I.  $N_2$  adsorption characteristics of porous silica samples.

<span id="page-1-0"></span>

	Gelsil 2.6	Gelsil 5	Vvcor	h	
Av. pore diameter (nm)	2.6	5.0			
Surface area $(m^2/g)$	586	509	72		
Pore volume $\left(\text{cm}^3/\text{g}\right)$	0.376	0.678	0.214		
Porosity $\phi$	0.51	0.66	0.30		FIG. 1. Sketch of (a) parallel plate and (b) three-point-bending

 $(DMA)<sup>36</sup>$  $(DMA)<sup>36</sup>$  $(DMA)<sup>36</sup>$  measurements in Vycor with  $d=7$  nm pore size. It turned out that the dynamic elastic response is very sensitive to the glass transition of liquids confined to mesoporous samples. Based on the results of computer simulations $29,37$  $29,37$ we could disentangle acceleration effects due to confinement and slowing down of molecular motion due to interaction of the molecules with the rough pore surface. We could even predict the pore size dependence of the dynamic elastic re-sponse (see Fig. 4 of Ref. [36](#page-8-22)). In order to test these predictions and to study the glass transition of salol for different pore sizes, further measurements have been performed. Here we present experimental results of the temperature and frequency dependence of the complex dynamic elastic susceptibility of salol confined in mesoporous matrices of *d*=7.5, 5.0, and 2.6 nm. In addition, thermal expansion measurements have been performed, which now allows us to take a new look at the often discussed negative pressure effect on glass forming liquids in confinement and to separate this effect from an intrinsic size effect.

The present paper is organized as follows: Sec. II yields insight into sample preparation and some technical details of DMA analysis. Section III displays a compilation of the experimental data and results of modeling and interpretation of the present data. It also contains a calculation of the effect of adsorption swelling and the separation of the actual downshift of  $T<sub>g</sub>$  in salol into the negative pressure effect and the confinement effect. Section IV concludes the paper.

#### **II. EXPERIMENT**

### **A. Sample preparation**

Porous Vycor samples are made by Corning Inc., NY and sold under the brand name "Vycor 7930." Via phase separation and leaching a three-dimensional random network of pores in nearly pure silica is fabricated.<sup>38</sup> Pores are uniformly distributed in length, direction, and density. $39$  The mean ratio of average pore diameter *d* and pore length *l* is  $d/l \approx 0.23$ . Gelsil is a mesoporous xerogel consisting of pure silica with a very narrow pore radius distribution. Gelsil rods were made by 4F International Co., Gainesville, FL. Results on pore sizes were derived from Barrett-Joyner-Halenda (BJH) analysis of the individual N<sub>2</sub>-desorption isotherms<sup>40</sup> and are summarized in Table [I.](#page-1-0)

All samples were cut and sanded in order to gain parallel surface plains. The typical size of a sample was  $(2 \times 2)$  $\times$  8) mm<sup>3</sup> for parallel plate and about (2  $\times$  1  $\times$  7) mm<sup>3</sup> for three-point-bending DMA measurements. Cleaning was done in a 30% hydrogen peroxide solution at 90 °C for 24 h,

<span id="page-1-1"></span>

geometry.

drying at 120 °C in a high-vacuum chamber at 10−6 bar, also for about 24 h. The guest glass forming material was salol (phenyl salicylate,  $C_{13}H_{10}O_3$ ), a low molecular weight liquid, whose melting temperature is  $T_m = 316$  K. Salol is a standard, so-called fragile, <sup>41</sup> glass former  $(m=73)$  known<sup>25</sup> to form a glass either at extreme cooling rates of 500 K/min or in pores smaller than 11.8 nm. Filling was done at 317 K via capillarity wetting. By comparing the weight of clean and filled samples the filling fractions  $f$  were determined (see Table [III](#page-6-0)).

### **B. Dynamic mechanical analysis**

In this method a static and a dynamic force  $F_{\text{stat}}$  $+ F_{dyn} \cdot e^{i\omega t}$  (0.001–16 N at 0.01–100 Hz) are applied on a sample using a quartz or steel rod (see Fig. [1](#page-1-1)). The response of the sample is measured via the displacement of the rod. Absolute height *h*, height amplitude  $\Delta h$ , and phase lag  $\delta$  are read via electromagnetic inductive coupling (LVDT) with a resolution of 10 nm and 0.01°, respectively. These data allow direct access to real and imaginary parts of the complex elastic susceptibility at low frequency and as a function of temperature and applied force. In addition, the thermal expansion of a sample can be determined in the so-called thermo mechanical analysis (TMA) mode, where no external force is applied. Two devices are used: A DMA 7 and a Diamond DMA, both from Perkin Elmer Inc. Two measuring geometries are applied: Parallel plate (PP) compression and three-point bending (3PB) (see Fig. [1](#page-1-1)).

Parallel plate geometry reveals purely the complex Young's modulus  $Y^* = Y' + iY''$ , where *Y'* and *Y''* are the storage and the loss modulus, respectively. The three-pointbending geometry delivers Young's modulus plus a small (geometry dependent) contribution of a shear elastic constant. More details on measurement geometry may be found in Refs. [42](#page-8-28) and [43.](#page-8-29) The absolute accuracy of resulting real and imaginary parts  $Y'$  and  $Y''$  is rather poor, mainly because of contact losses between the quartz rod and the sample. A discussion of these systematic errors may be found in Ref. [36.](#page-8-22) In contrast the relative accuracy is excellent and the DMA method is estimated to be about 100 times more sensitive to detect glass transitions or other subtle phase transitions than differential scanning calorimetry (DSC) measurements[.44](#page-8-30)

## **III. RESULTS AND DISCUSSION**

#### **A. Dynamic elastic response**

Diamond DMA measurements (in parallel plate and threepoint-bending geometry) of Vycor and Gelsil samples filled

<span id="page-2-1"></span><span id="page-2-0"></span>

FIG. 2. Real (a) and imaginary parts (b) of the complex Young's modulus of Vycor 7.5 nm filled with salol (filling fraction  $f \approx 0.79$ ) measured in three-point-bending geometry. The curves are offset

with salol are shown in Figs. [2–](#page-2-0)[5.](#page-3-0) The loss modulus *Y*" [Fig.  $2(b)$  $2(b)$ ] of salol in 7.5 nm pores clearly shows a "two-peak structure," i.e., a peak with half-width at half maximum (HWHM) about 20 K, and a shoulder or second peak at about 1[5](#page-3-0) K higher temperature [also see Fig.  $5(b)$ ]. This is also reflected by the real part *Y*, which displays a "two-steplike shape" with temperature [Figs.  $2(a)$  $2(a)$  and  $5(a)$  $5(a)$ ]. Both peaks in Y'' shift to higher temperatures with increasing frequency as expected for a glass transition. In smaller pores of Gelsil 5.0, peak and shoulder merge into one asymmetric peak of width  $\sim$  [3](#page-2-1)0 K [see Figs. 3(b) and [5](#page-3-0)(e)], also shifted with higher frequency to higher temperatures. In 2.6 nm pores the loss peak shows a rather symmetric form broadened up to about 60 K [see Figs.  $4(b)$  $4(b)$  and  $5(f)$  $5(f)$ ].

While in large pores of 7.5 nm diameter vitrification of salol seems to happen decoupled (two peaks in *Y*") in regions near the pore surface and the pore center; things change in smaller pores. With decreasing pore diameter, *Y*<sup>"</sup> approaches a symmetric form and simultaneously *Y'* changes from a "double step shape" into a "single step shape," indicating only one type of relaxation process. Similar broadening effects as for the loss peaks of our DMA measurements were observed in pores of decreasing size also by calorimetric<sup>23</sup> and dielectric measurements. $45,46$  $45,46$  This broadening as well as a shift of the glass transition to lower temperatures was calculated by Sappelt and Jäckle $47$  using kinetic Ising and lattice gas models, and shown to originate from confinement induced suppression of cooperative motion of molecules.

Pure Vycor and Gelsil, meaning exposed to air and therefore mostly filled with nitrogen, do not show any of these features. *Y* decreases about 2% between 300 and 180 K. *Y*-



FIG. 3. Real (a) and imaginary (b) parts of the complex Young's modulus of Gelsil 5.0 nm filled with salol (filling fraction  $f \approx 0.75$ ) measured in parallel plate geometry (Diamond DMA). The 1 Hz signal is original data; other signals are offset for sake of clarity.

is constant within the corresponding temperature range.

Any standard relaxation model like Debye, Kohlrausch, Cole-Cole or Cole-Davidson fails to describe our dynamic elastic susceptibility data if only one type of relaxation process is assumed. One would have to use extreme stretching parameters to fit *Y*, which then leads to improper temperature shifts of the peaks in Y'' with respect to the experimental data and misfitting signal heights. The most efficient model to describe our data turned out to be a modification of the empirical Vogel-Fulcher-Tammann law

$$
\tau(T) = \tau_0 \cdot \exp\left[\frac{E}{T - T_0}\right],\tag{1}
$$

<span id="page-2-2"></span>where  $\tau_0$  is a preexponential factor,  $E \cdot k_B$  is an activation energy, and  $T_0$  is the Vogel-Fulcher (VF) temperature. Following computer simulations $29,37$  $29,37$  we take into account a shift of VF temperatures along the pore radius *r*. In a recent paper Zorn *et al.*<sup>[27](#page-8-13)</sup> suggest the empirical ansatz

$$
T_0(r) = T_{00} + \frac{k}{R - r + r_p},\tag{2}
$$

<span id="page-2-3"></span>with the bulk VF temperature  $T_{00}$ , and the pore radius *R*  $=$ *d*/2. The so-called penetration radius  $r_p$  is the radius be-

<span id="page-3-1"></span>

FIG. 4. Real (a) and imaginary (b) parts of the complex Young's modulus of Gelsil 2.6 nm filled with salol (filling fraction  $f \approx 0.65$ ) measured in three-point-bending geometry (Diamond DMA). The 1 Hz signal is original data; other signals are offset for sake of clarity.

<span id="page-3-0"></span>yond which it is very unlikely to find a particle in the fluid state.<sup>[2](#page-2-3)9</sup> The combination of Eqs.  $(1)$  $(1)$  $(1)$  and  $(2)$  leads to a radial

<span id="page-3-2"></span>distribution of relaxation times  $\tau$  inside the pore:

$$
\tau(r,T) = \tau_0 \cdot \exp\left[\frac{E}{T - \left(T_{00} + \frac{k}{R - r + r_p}\right)}\right].
$$
 (3)

Equation  $(3)$  $(3)$  $(3)$  describes the exponential increase in relaxation time when a rough pore wall is approached, and a growing influence of the pore wall with decreasing temperature, a behavior which was also found by recent computer simulations[.8,](#page-7-9)[29](#page-8-15)[,37](#page-8-23)[,48](#page-8-34) A temperature parametrized Cole-Cole plot of *Y*<sup>*''*</sup> vs *Y*<sup>*'*</sup> of our data calls for a Cole-Davidson model of the complex dynamic elastic susceptibility

$$
Y^*(\omega) \propto \frac{1}{(1 + i\omega\tau)^{\gamma/2}},\tag{4}
$$

<span id="page-3-5"></span>with  $\omega = 2\pi \nu$ ,  $\nu$  being the measurement frequency, and the broadening parameter  $\gamma$ . Using Eq. ([3](#page-3-2)), averaging over the pore radius *R*, and separating real and imaginary part of *Y*  $=Y' + i \cdot Y''$  by common procedures leads to

<span id="page-3-3"></span>
$$
Y' = 1 - \frac{2\Delta Y}{R^2} \int_0^R \frac{\cos[\gamma \cdot \arctan(\omega \tau(r, T))] }{[1 + \omega^2 \tau(r, T)^2]^{1/2}} r dr, \quad (5a)
$$

$$
Y'' = \frac{2\Delta Y}{R^2} \int_0^R \frac{\sin[\gamma \cdot \arctan(\omega \tau(r, T))] }{[1 + \omega^2 \tau(r, T)^2]^{\gamma/2}} r dr.
$$
 (5b)

<span id="page-3-4"></span>As already mentioned above, the two-peak structure in *Y*<sup>*n*</sup> of 7.5 and 5 nm confined salol (Figs.  $2$  and  $3$ ) suggests to split the dynamic elastic response into a core and a surface contribution: The molecules in the core (center of the pores) behave bulklike and are dynamically decoupled from the molecules near the pore surface. This is modeled by inserting into Eqs.  $(5a)$  $(5a)$  $(5a)$  and  $(5b)$  $(5b)$  $(5b)$  the corresponding relaxation times  $\tau_0$ ·exp[ $E/(T-T_0)$ ] given by Eq. ([1](#page-2-2)) if  $r \le R_c$  and  $\tau(r,T)$ given by Eq. ([3](#page-3-2)) if  $r > R_c$  (see also Fig. [7](#page-4-0)). The sum of the two contributions perfectly describes our *Y*<sup>*'*</sup> and *Y*<sup>*''*</sup> data on



FIG. 5. Real (a) and imaginary (b) parts of the complex Young's modulus of salol in Vycor or Gelsil for different pore sizes, all measured at 20 Hz.

<span id="page-4-1"></span>

FIG. 6. Real part *Y'* and imaginary part *Y''* of different porous samples filled with salol. The lines are fits using Eqs. ([5a](#page-3-3)) and ([5b](#page-3-4)) with parameters of Table [II.](#page-4-2)

salol in 7.5 and 5 nm pores simultaneously (see Fig.  $6$ ).

In 2.6 nm pores we do not expect any molecule to behave like the bulk liquid any more, since the pore radius is of the same order as the estimated surface shell (see Table  $II$ ), implying that every molecule is influenced by the near surface. Therefore we use Eqs.  $(5a)$  $(5a)$  $(5a)$  and  $(5b)$  $(5b)$  $(5b)$  with no bulk term which reproduces one single peak and also fits our data very well [Figs.  $5(c)$  $5(c)$  and  $5(f)$  and Figs.  $6(c)$  $6(c)$  and  $6(f)$ ].

The radius of the "core" of bulklike interacting molecules turned out to be  $R_c$ =2.5 nm and 1.35 nm in 7.5 nm and 5.0 nm pores, respectively (see Table  $II$ ). This implies that the thickness of the shell of molecules being slowed down by wall interaction  $R-R_c=1.25$  nm and 1.15 nm for 7.5 nm and 5.0 nm pores, respectively.

Additional loss peaks, attributed to molecules forming H bonds to the inner pore surface, have also been reported from dielectric measurements of salol in 7.5 nm pores. $49,50$  $49,50$  The work of Kremer and Stannarius<sup>50</sup> also revealed that the typical size of a shell of molecules interacting with the pore surface is about 2 or 3 molecules. Since the size of a salol molecule is estimated as  $(1.4 \times 0.6 \times 0.4)$  nm<sup>3</sup> in Ref. [51](#page-8-26) or as  $0.282 \text{ nm}^3$  in Ref. [52,](#page-8-37) both corresponding to a mean diameter of 0.8 nm, this shell size is on the order of 1.6 to 2.4 nm. This is in very good agreement with our findings (see

TABLE II. Fit parameters used in Eqs.  $(5a)$  $(5a)$  $(5a)$  and  $(5b)$  $(5b)$  $(5b)$  for fits of Fig. [6.](#page-4-1)

<span id="page-4-2"></span>

	Vycor	Gelsil 5	Gelsil 2.6
$R$ (nm)	3.75	2.50	1.28
$r_p$ (nm)	0.36	0.25	0.28
E(K)	1750	1750	1750
$T_{00}$ (K)	158.5	156.2	136.0
$\tau_0$ (s)	$10^{-11}$	$10^{-11}$	$10^{-11}$
$\gamma$	0.33	0.18	0.15
$k$ (nm K)	18	11	25
$R_c$ (nm)	2.5	1.35	
Shell $R - R_c$ (nm)	1.25	1.15	1.28

Table  $\Pi$ ). The core size  $R_c$  decreases with decreasing pore radius (see Table [II](#page-4-2) and Fig. [7](#page-4-0)), also in very good agreement with the results of Kremer *et al.*[26](#page-8-12)

The fitted Vogel-Fulcher temperature  $T_{00}$  is reduced with respect to the bulk and with decreasing pore size (see Table [II](#page-4-2)). In order to compare our results with published data, we plotted the relaxation time in the pore center  $\tau(r=0, T)$  for various pore sizes *d* and determined the corresponding  $T_g(d)$ by using the common procedure<sup>53</sup> for finding the laboratory glass transition temperature, i.e., a cut with a horizontal line at  $\tau = 100$  s (see Fig. [8](#page-5-0)). As shown in Fig. [11,](#page-7-14) this leads to glass transition temperatures decreasing  $\alpha$ 1/*d* in very good agreement with published data of DSC measurements.<sup>28</sup>

On the other hand there are molecular dynamics simulations<sup>32,[33](#page-8-19)</sup> of glass forming liquids pointing to the fact that at higher temperatures above the mode coupling temperature  $T_c = 260$  K of salol<sup>54</sup> confinement slows down the dynamics. However within the present experimental frequency range  $(0.01-100 \text{ Hz})$  we are not able to detect such a crossover to confinement induced slowing down by heating the sample from  $T_g$  to temperatures above  $T_c$  for the following reason: An extrapolation of the relaxation times of Fig. [8](#page-5-0) to these temperatures shows that  $\tau(T > 260 \text{ K}) < 10^{-4} \text{ s, im}$ plying that  $\omega \tau \leq 1$  within this temperature range even at the

<span id="page-4-0"></span>

FIG. 7. Modeled relaxation time distributions in pores of diameter 7.5 nm to 2.6 nm from Eq.  $(3)$  $(3)$  $(3)$  used in Eqs.  $(5a)$  $(5a)$  $(5a)$  and  $(5b)$  $(5b)$  $(5b)$  for fits of Fig. [6.](#page-4-1)

<span id="page-5-0"></span>

FIG. 8. Relaxation time in pore centers calculated from Eqs.  $(1)$  $(1)$  $(1)$ and  $(3)$  $(3)$  $(3)$  with corresponding parameters from Table [II.](#page-4-2) The horizontal line shows  $\tau = 100$  s.

highest available measurement frequency of 100 Hz. Therefore the dynamic elastic susceptibility given by Eq.  $(4)$  $(4)$  $(4)$  is actually independent of  $\tau$  and we have to extend our frequency range to higher frequencies. Work in this direction using resonant ultrasound spectroscopy (RUS, 50 kHz $<$  $\nu$  $<$  1.5 MHz) is in progress.

#### **B. Filling process and accompanying effects**

By using a DMA in a static TMA mode one can detect small changes in a sample's height with a resolution of 10 nm. We measured the time dependent swelling of the Vycor and Gelsil samples during filling with salol and the thermal expansion of empty and filled samples in the following way: In parallel plate mode, the quartz rod is placed on top of the sample with force  $F=0$  N, and just height and temperature signals are read out. A clean piece of Vycor/ Gelsil sample is cooled down to 170 K. Afterwards the sample is heated slightly above the melting temperature  $T_m$ =316 K of salol and kept there isothermally. Crystalline, powderlike salol placed right around the sample melts and percolates the Vycor/Gelsil sample due to capillarity (Fig. [9](#page-5-1)). After filling until saturation, the sample is cooled down to 170 K again (Fig.  $10$ ). The time dependence of the filling process is displayed in Fig. [9](#page-5-1) for Vycor. While salol is percolating the sample, the temperature is held constant and the sample's height is measured. Charts for Gelsil 5.0 nm and Gelsil 2.6 nm look very similar. The diagrams in all cases show the typical  $\sqrt{t}$  behavior as expected for a single capillary rise experiment, following Lucas<sup>55</sup> and Washburn.<sup>56</sup> This result is in concordance with findings of Huber *et al.*, [57](#page-8-42)

<span id="page-5-1"></span>

FIG. 9. Height of Vycor sample during the filling process against  $\sqrt{t}$ . The inset shows sample height against time.

who investigated the mass uptake of porous silica samples and its time dependence, leading to the Lucas-Washburn  $\sqrt{t}$ behavior of the mass uptake with time. Very recently it was shown that the Lucas-Washburn equation (with small modifications) works well even at the nanoscale,<sup>58</sup> which is in harmony with our results.

The expansion of a porous sample during adsorption of gases or water has already been investigated in the 1920s.<sup>59</sup> As a liquid/gas intrudes the sample it is subject to a negative hydrostatic pressure inside the pores, which leads to an expansion of the porous sample during adsorption of gases or water. Mesoporous media have enormous inner surfaces up to some 100  $\mathrm{m}^2/\mathrm{g}$  (see Table [I](#page-1-0)). This leads to a considerable stress reduction within the whole matrix and a sudden voluminal growth, which slows down and stops as all pore space is filled (see Fig. [9](#page-5-1)). The change in height due to the adsorption swelling can even be calculated quantitatively. The pressure reduction of the liquid in a capillary is known<sup>60</sup> as  $P_c$  $=2\sigma/r$ , with the surface tension  $\sigma$  and the capillary radius *r*. With  $\sigma$ =1.73×10<sup>-2</sup> N/m from Ref. [28,](#page-8-14) this yields a capillary pressure of 26.6 MPa in 2.6 nm pores. This would lead to a hypothetical capillary rise of 1.8 km for salol. The linear strain  $\epsilon = \Delta h/h$  accompanying the filling process can be computed by the equation $61$ 

$$
\epsilon = \frac{f \cdot P_c}{3} \left( \frac{1}{K} - \frac{1}{K_s} \right) \tag{6}
$$

<span id="page-5-3"></span>with the filling fraction  $f$ , the bulk modulus  $K$  of the empty host matrix, and the bulk modulus of the material building

<span id="page-5-2"></span>

FIG. 10. Linear thermal expansion of empty and salol filled samples with pore diameters of (a) 7.5 nm, (b) 5.0 nm, and (c) 2.6 nm.

<span id="page-6-0"></span>

	Vycor	Gelsil 5	Gelsil 2.6
$d$ (nm)	7.5	5.0	2.6
Porosity $\Phi$	0.31	0.66	0.51
$P_c$ (MPa)	9.2	13.8	26.6
K(GPa)	8.1	3.9	9.6
f	0.77	0.62	0.32
$\epsilon_{\rm calc}$	$2.3 \times 10^{-4}$	$6.6 \times 10^{-4}$	$2.2 \times 10^{-4}$
$\epsilon_{\rm exp}$	$1.0 \times 10^{-4}$	$4.1 \times 10^{-4}$	$3.5 \times 10^{-4}$

TABLE III. Variables of Eq. ([6](#page-5-3)).

the solid frame  $K_s$  (which is nearly pure  $SiO_2$ ). The bulk moduli  $K$  have been determined by RUS.<sup>62</sup> Table [III](#page-6-0) shows parameters used to calculate  $\epsilon = \Delta h/h$ . The calculated values for the adsorption swelling agree rather well with the experimental results.

#### **C. Negative pressure effect**

The downshift of the glass transition in nm-confining pores is often reported to obey a  $1/d$  law (see Refs. [23,](#page-8-9) [25,](#page-8-11) [28,](#page-8-14) and [63](#page-8-48)). At first this was proposed by Jackson and McKenna,<sup>23</sup> following their former results on the shift of the melting transition  $T_m$  in confinement.<sup>64</sup> But the supposed suppression of molecular cooperation when the pore diameter approaches an inherent length scale is not the only possible reason for a downward shift of  $T_g$  in confinement. Zhang *et al.*<sup>[63](#page-8-48)</sup> proposed the increase in negative hydrostatic pressure within the pores due to mismatching thermal expansions of liquid and host matrix as the main driving force for the downshift of  $T<sub>g</sub>$ . This idea was also discussed by Patkowski *et al.*[28](#page-8-14) and Simon *et al.*, [65](#page-8-50) and was reviewed by Alcoutlabi and McKenna[.34](#page-8-20)

As Fig.  $10(a)$  $10(a)$  shows, for large pores and in a cooling process starting at RT, at higher temperatures the Vycor matrix is not affected by its filling. It contracts like the empty Vycor matrix with a thermal expansion coefficient  $\alpha$  $=\Delta h/(h \cdot \Delta T)$ =5.1×10<sup>-6</sup> K<sup>-1</sup>. Patkowski *et al.*<sup>[28](#page-8-14)</sup> proposed the possible flow and equilibration of the confined liquid well above  $T_g$ , which we also consider to be the case here. But as vitrification sets in at about 230 K, the filled Vycor matrix is subject to a contraction which is stronger compared to the empty Vycor sample. Strong interaction (H bondings) between salol and the pore surface might be the reason for this. At smaller pores of filled Gelsil samples [Figs.  $10(b)$  $10(b)$ and  $10(c)$  $10(c)$ ] additional contraction already starts at higher temperatures. For an estimation of the process developing negative pressure upon the filling liquid, the strain misfit between the glass and the host matrix is

$$
\Delta \epsilon^{mf} = 3(\alpha_1 - \alpha_2) \Delta T \tag{7}
$$

with  $\alpha_i$ , the thermal expansion coefficients of the host matrix (1) and salol (2). Negative pressure then derives from  $\Delta P$  $=\Delta \epsilon / \kappa_T$ , where  $\kappa_T$  is the bulk compressibility of salol. The resulting shift of  $T_g$ , i.e.,

TABLE IV. Parameters of  $\Delta T_g$  estimations,  $\Delta T_g^{exp} = \Delta T_g^{np}$  $+\Delta T\frac{\text{conf}}{g}$ .

<span id="page-6-1"></span>

	Vycor	Gelsil 5.0	Gelsil 2.6
$d$ (nm)	7.5	5.0	2.6
$\alpha_2$ (K <sup>-1</sup> )	$2.1 \times 10^{-5}$	$4.6 \times 10^{-5}$	$1.1 \times 10^{-5}$
$\Delta T$ (K)	6	10	15
$\Delta \epsilon^{mf}$ (%)	$-0.40$	$-0.60$	$-1.06$
$\Delta P$ (MPa)	$-8.1$	$-12.0$	$-21.1$
$\Delta T_g^{np}$ (K)	$-1.6$	$-2.4$	$-4.3$
$\Delta T^{\rm conf}_g$ (K)	$-1.4$	$-2.9$	$-6.4$
$\Delta T^{\,\rm exp}_{\,g}\,$ (K)	$-3.0$	$-5.3$	$-10.7$

$$
T_g(P) = T_g(P=0) \left. \frac{\partial T_g}{\partial P} \right|_{P=0} \cdot \Delta P \tag{8}
$$

crucially depends on the choice of  $\Delta T$ , the temperature range, in which the effective negative pressure upon salol develops. This effective temperature range can be estimated from our data as follows: As calculated from Eq.  $(6)$  $(6)$  $(6)$  the host porous matrix expands with filling due to the negative capillary pressure which acts on the confined liquid. Since with cooling the liquid salol contracts, this stress relaxes and the composite is stress free if the filled sample height is the same as for the empty matrix which occurs at  $T = T^*$  (see Fig. [10](#page-5-2)). So  $\Delta T \approx T^* - T_g$ . Results of these estimations are given in Table [IV.](#page-6-1) Parameters used for salol are  $\kappa_T = 5 \times 10^{-10}$  Pa<sup>-1</sup> from Ref. [66,](#page-8-51) the thermal expansion coefficient  $\gamma_1 = 3\alpha_1$  $=7.36\times10^{-4}$  K<sup>-1</sup> from Ref. [1,](#page-7-3) and  $\partial T_g / \partial P = 0.204$  K/MPa from Ref. [67.](#page-8-52) Our measurements are in accordance with enthalpy recovery results of Simon *et al.*[65](#page-8-50) Their model shows that effective negative pressure develops 2 to 2.5 K above the reduced glass transition for samples with 11.6 and 25.5 nm pore sizes. Further, they state "...If negative pressure were the cause of the depressed  $T_g$ , the temperature at which isochoric conditions are imposed would have to be  $\sim$  20 to 40 K above  $T<sub>g</sub>$ ." For comparison we obtain a necessary  $\Delta T$  $=10$  to 40 K for  $d=7.5$  to 2.6 nm pores, which is in very good agreement with Simon *et al.*

In our opinion our calculated  $\Delta T_g^{np}$  is still overestimated for two reasons: First, using the bulk value  $\alpha_2$  of the host matrix from Fig. [10](#page-5-2) does not take into account internal pore walls being affected by the negative pressure inside, relaxing to some extent and so reducing pressure. Second, thermal expansions of other glass forming liquids, e.g., toluene have been reported 1.5 times smaller in confinement<sup>68</sup> compared to bulk. Moreover, thermal expansion of liquid salol drops<sup>1</sup> to a *quarter* of its value at the glass transition. So, as the glass transition sets in,  $\alpha_1$  starts to decrease and a purely pressure induced downshift  $\Delta T_g$  would be even more diminished. Apart from this the reason for the size dependence of the thermal mismatch effect (see Fig. [11,](#page-7-14) open circles) is not clear at all.

#### **IV. CONCLUSIONS**

The glass transition of salol confined to porous host matrices of Vycor and Gelsil with pore sizes of 7.5, 5.0 and 2.6

<span id="page-7-14"></span>

FIG. 11. Shift of glass transition temperature against (pore diameter)<sup>-1</sup>. The boxes are  $T_g$ 's from Fig. [8,](#page-5-0) triangles show literature values from Ref. [28,](#page-8-14) and open circles display the maximum negative pressure contribution (see Sec. III C).

nm has been measured by Dynamic Mechanical Analyzers (DMA 7 and Diamond DMA, Perkin Elmer). The dynamic complex elastic susceptibility data can well be fitted assuming two types of dynamic processes: A "bulk" relaxation in the core of the pores and a radially increasing "surface relaxation" of molecules near the pore surface. The calculated core relaxation time shows a typical Vogel-Fulcher temperature dependence and decreases with decreasing pore size *d*. This confinement induced acceleration of dynamics leads to a shift of the glass transition temperature  $T_g \propto 1/d$ , which is in perfect agreement with recent DSC results.<sup>28</sup> Measurements of the sample height with filling (adsorption swelling) and thermal expansion are used to calculate the effect of "negative pressure" due to thermal mismatch between the porous host matrix and the glass forming liquid. Such negative pressure could at least partly explain a shift of  $T_g$  in confined glass forming liquids. $28,34,65$  $28,34,65$  $28,34,65$  Our data show that for salol this effect of thermal mismatch could describe at most 30% of the observed downshift of  $T_g$ , which is in harmony with enthalpy recovery experiments.<sup>65</sup>

In our opinion the main cause for the shift of  $T<sub>g</sub>$  is a hindering of cooperativity due to confinement. This is also supported by an estimation of this effect using the results of Hunt *et al.*<sup>[69](#page-8-54)</sup> They calculated the finite-size effect of the glass transition from percolation and effective medium models, which yields

$$
T_g(d) = T_g(\text{bulk}) - \frac{0.5 \cdot E}{\ln(t \cdot \nu_{\text{ph}})} \cdot \frac{r_0}{L}.
$$
 (9)

<span id="page-7-15"></span>Inserting  $t=100$  s,  $v_{ph}=1/\tau_0$ , and our fit parameters from Table [II,](#page-4-2) and assuming that the typical distance between molecules  $r_0$  is about the diameter of a salol molecule<sup>52</sup>  $(d_0)$  $\approx$  0.8 nm), we obtain  $\Delta T_g^{\text{Hunt}}$  as 3.2, 4.8 and 9.1 K for 7.5, 5.0 and 2.6 nm pores, respectively. These calculated values agree surprisingly well with the measured confinement induced downshifts of  $T_g(d)$  (see Fig. [11](#page-7-14) and  $\Delta T_g^{\text{exp}}$  in Table [IV](#page-6-1)).

Moreover Eq.  $(9)$  $(9)$  $(9)$  predicts<sup>69</sup> that the size dependence of  $\Delta T_g$  increases with increasing fragility,<sup>70</sup>

$$
m = \frac{E \cdot T_g}{\ln(10)(T_g - T_0)^2},\tag{10}
$$

since  $m \propto E$ . Indeed, this correlation between  $\Delta T_g(d) \sim m$  was verified experimentally for many systems, i.e., for glycerol $63$  $(m=53)$   $\Delta T_g$   $(d=2.5 \text{ nm}) \approx -4 \text{ K}$ , benzyl-alcohol<sup>23</sup> *(m*)  $=65$ ) ΔT<sub>g</sub> (d=2.5 nm)≈-9 K, salol<sup>28</sup> (m=73) ΔT<sub>g</sub> (d  $(2.5 \text{ nm})^2 \approx -11 \text{ K}$ , *o*-terphenyl<sup>28</sup>  $(m=81)$   $\Delta T_g$   $(d=81)$  $= 2.5$  nm)  $\approx -25$  K.

We think that these considerations, i.e., the downshift of  $T<sub>g</sub>$  calculated via percolation theory, as well as the clear correlation between the magnitude of induced  $T<sub>g</sub>$  shift and the fragility of a glass forming liquid, both confirm our other findings (see Fig.  $11$ ) that the main effect of the confinement is to suppress cooperative motion. Negative pressure effects although always present contribute only little.

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